

# The PM Programming Language

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IMPLEMENTING NUMERICAL MODELS ON DISTRIBUTED HARDWARE

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# Research/HPC Software Divide

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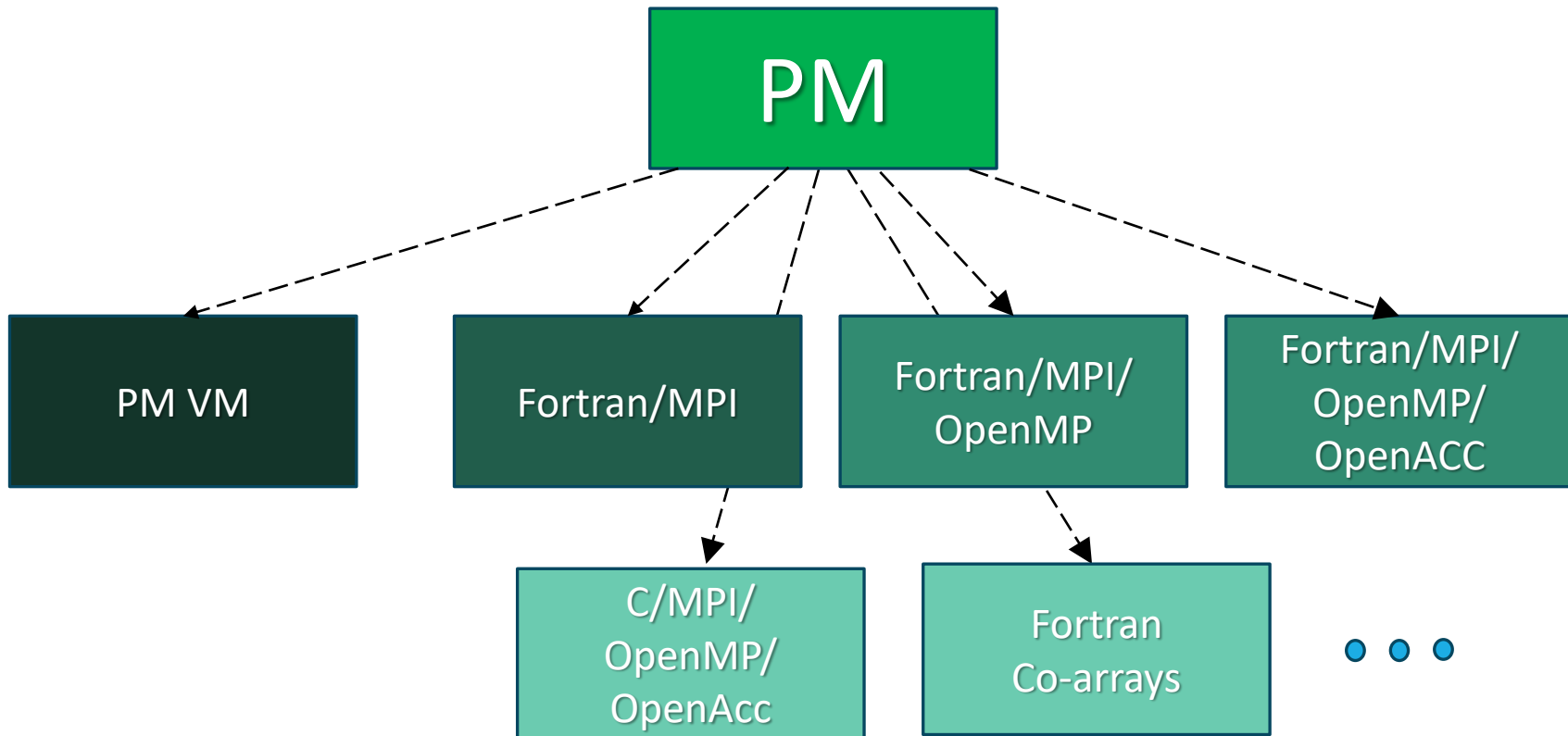
Python / Matlab / ...

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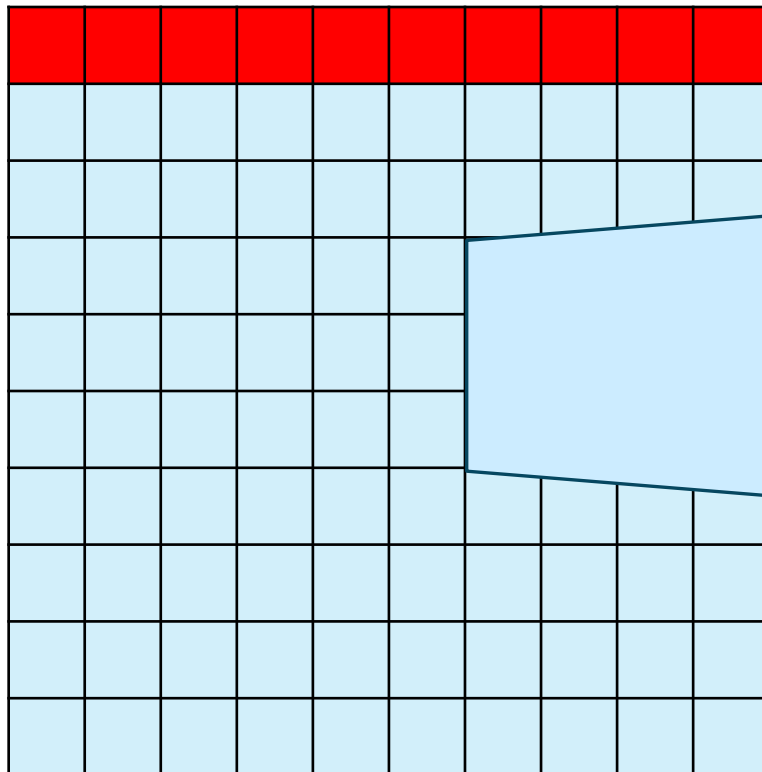
FORTRAN/C/C++  
+ MPI + OpenMP  
+ OpenAcc/CUDA/...

# PM Programming Language

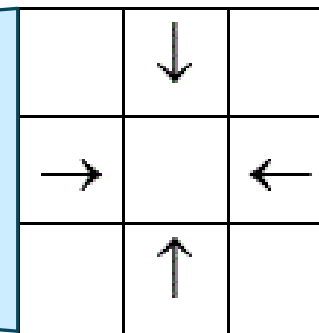
New programming language and programming language implementation designed for numerical modelling on distributed systems



# An example model



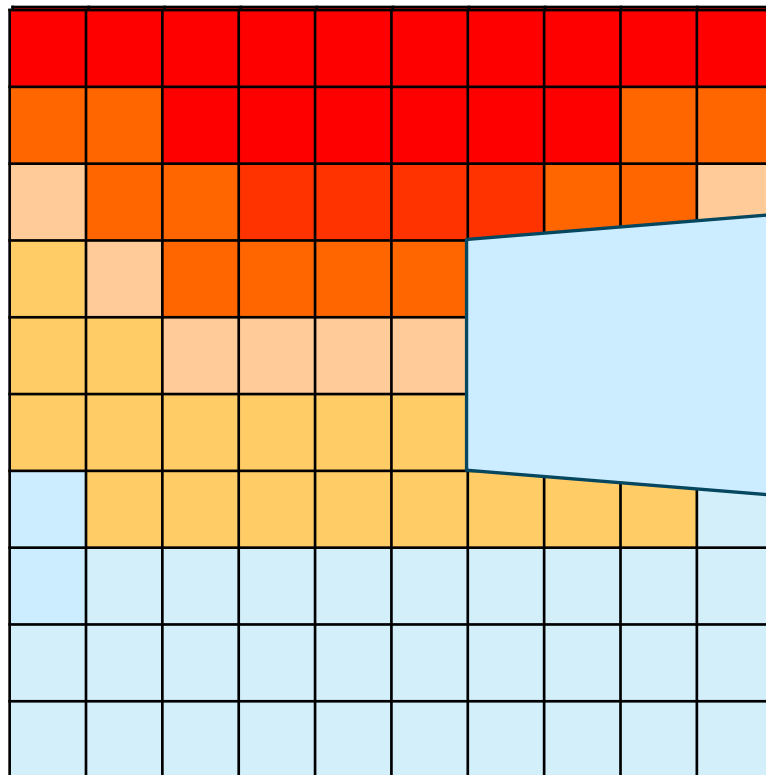
Jacobi iterative solution to 2D heat equation  $\nabla^2 x = 0$



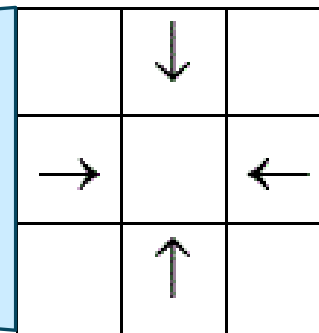
$$x_{i,j} = \frac{x_{i+1,j} + x_{i-1,j} + x_{i,j+1} + x_{i,j-1}}{4}$$

Repeat until no further change

# An example model



Jacobi iterative solution to 2D heat equation  $\nabla^2 x = 0$

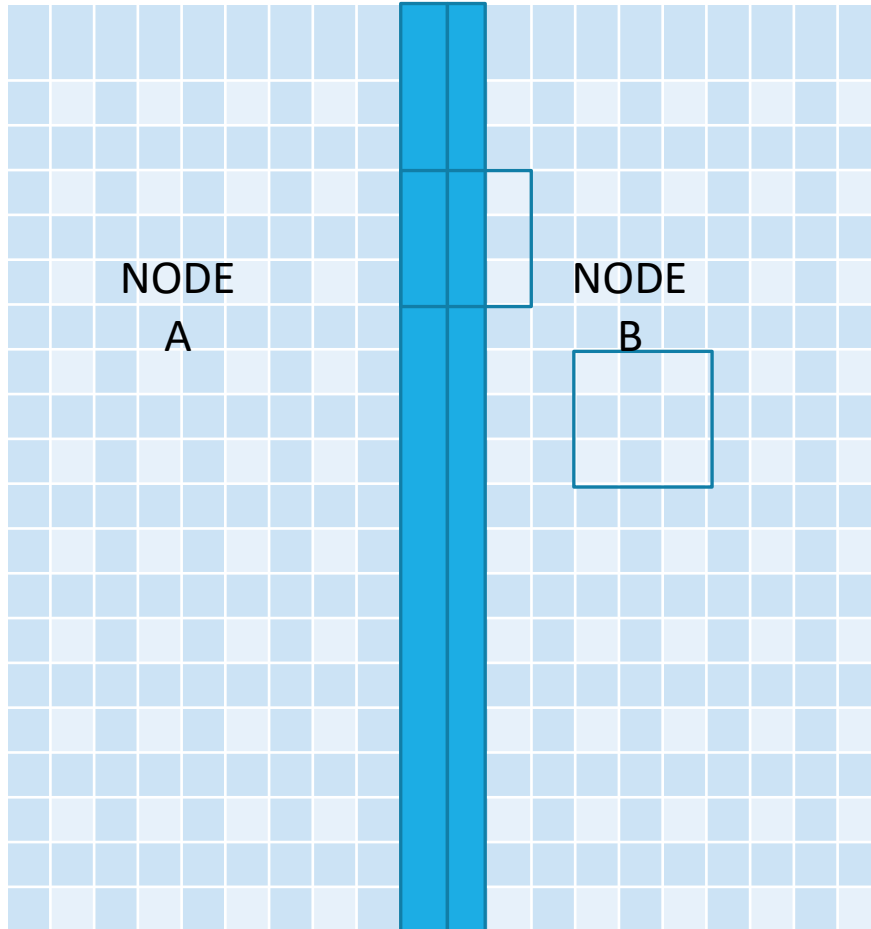


$$x_{i,j} = \frac{x_{i+1,j} + x_{i-1,j} + x_{i,j+1} + x_{i,j-1}}{4}$$

Repeat until no further change

# Distribution

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# Coding models in PM

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```
var out_array=darray(0.0,[0..MODEL_COLS+1,0..MODEL_ROWS+1])
for x in out_array {
  over [0,]: x=1.0
  until invar totdiff<TOL {
    var diff=0.0
    nhd [-1..1,-1..1] dx of x bounds EXCLUDED {
      cell=(dx[-1,0]+dx[1,0]+dx[0,-1]+dx[0,1])/4.0
      diff=(x-dx[0,0])**2
    }
    totdiff=sqrt(sum%(diff)/size(out_array))
  }
}
```

# Coding models in PM

```
var out_array=darray(0.0,[0..MODEL_COLS+1,0..MODEL_ROWS+1])
for x in out_array {
  over [0,]: x=1.0
  until invar totdiff<TOL
  var diff=0.0
  nhd [-1..1,-1..1] dx
  cell=(dx[-1,0]+dx[1,0]+dx[0,-1]+dx[0,1])/4.0
  diff=(x-dx[0,0])**2
}
totdiff=sqrt(sum%(diff)/size(out_array))
}
```

Extensive, optional, compile-time type inference



# Coding models in PM

```
var out_array=darray(0.0,[0..MODEL_COLS+1,0..MODEL_ROWS+1])
for x in out_array {
  over [0,]: x=1.0
  until invar totdiff<TOL {
    dx of x bounds EXCLUDED {
      dx[1,0]+dx[0,-1]+dx[0,1])/4.0
      diff=(x-dx[0,0])**2
    }
    totdiff=sqrt(sum%(diff)/size(out_array))
  }
}
```

Explicitly parallel  
statements

# Coding models in PM

```
var out_array=darray(0.0,[0..MODEL_COLS+1,0..MODEL_ROWS+1])
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  until invar totdiff<TOL {
    var diff=0.0
    nhd [-1..1,-1..1] dx of x bounds EXCLUDED {
      cell=(dx[-1,0]+dx[1,0]+dx[0,-1]+dx[0,1])/4.0
      diff=(x-dx[0,0])**2
    }
    totdiff=sqrt(sum%(diff)/size(out_array))
  }
}
```

Operations that  
communicate between  
parallel strands

# Scope

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```
if x < 0 {
```

```
    var outer = 1
```

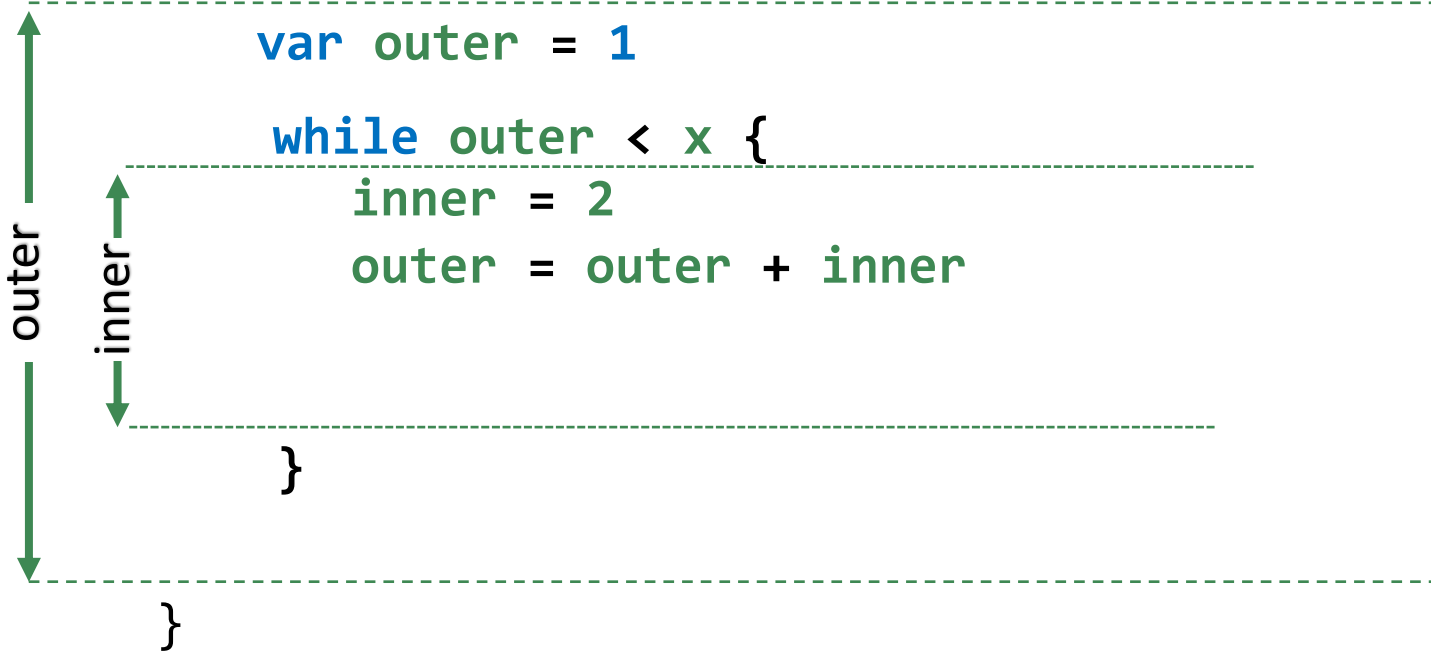
```
    while outer < x {
```

```
        inner = 2
```

```
        outer = outer + inner
```

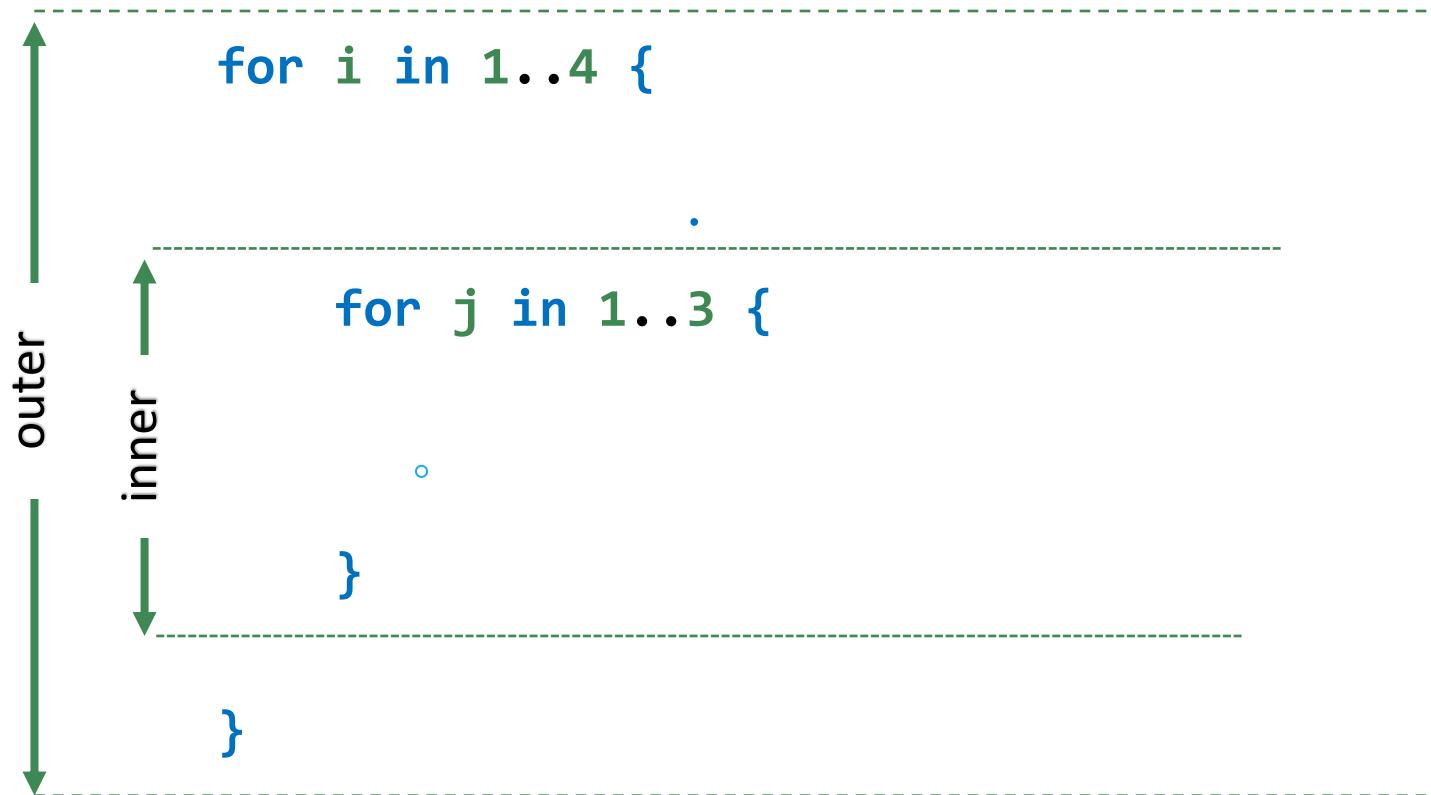
```
    }
```

```
}
```



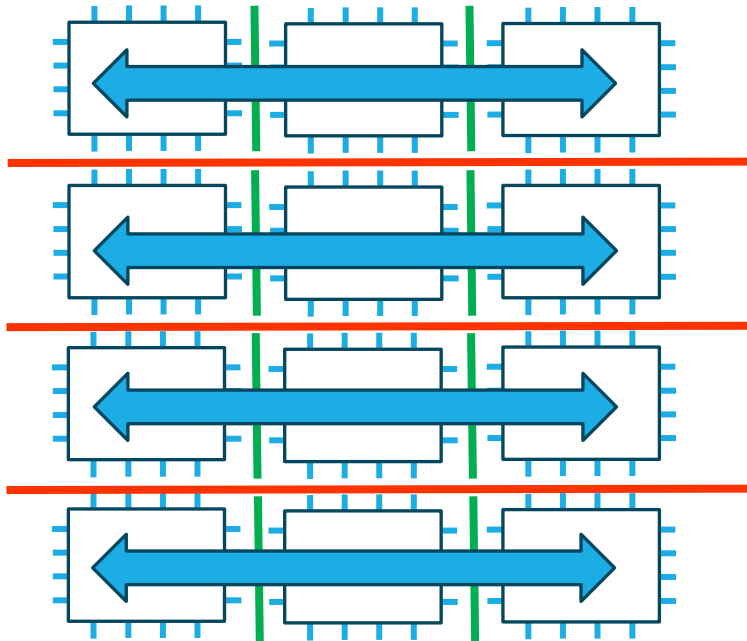
# Parallel Scope

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# Parallel Scope

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```
for i in 1..4 {
```

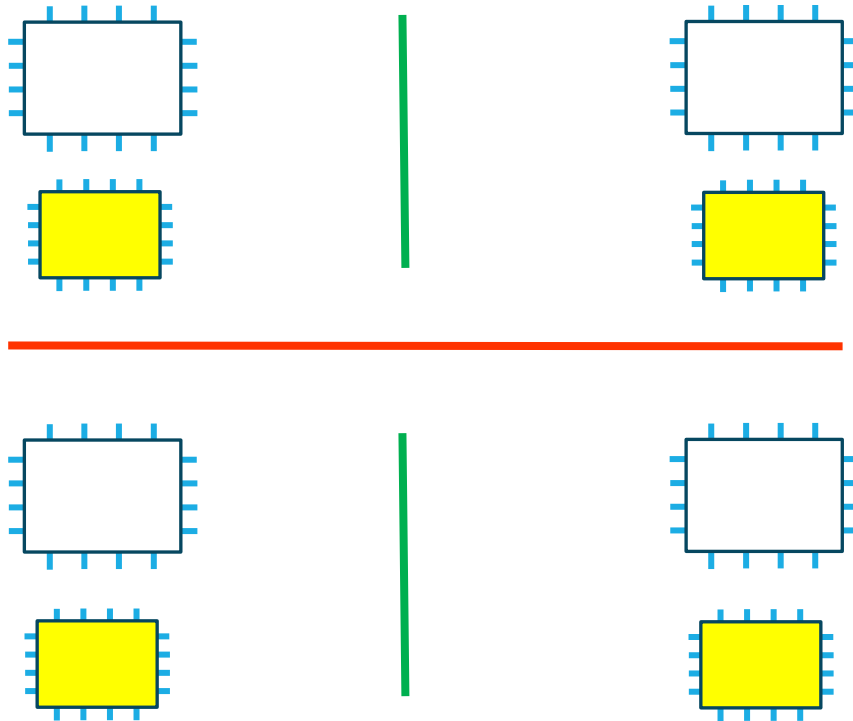
```
  for j in 1..3 {
```

```
  }
```

```
}
```

# Adding accelerators\*

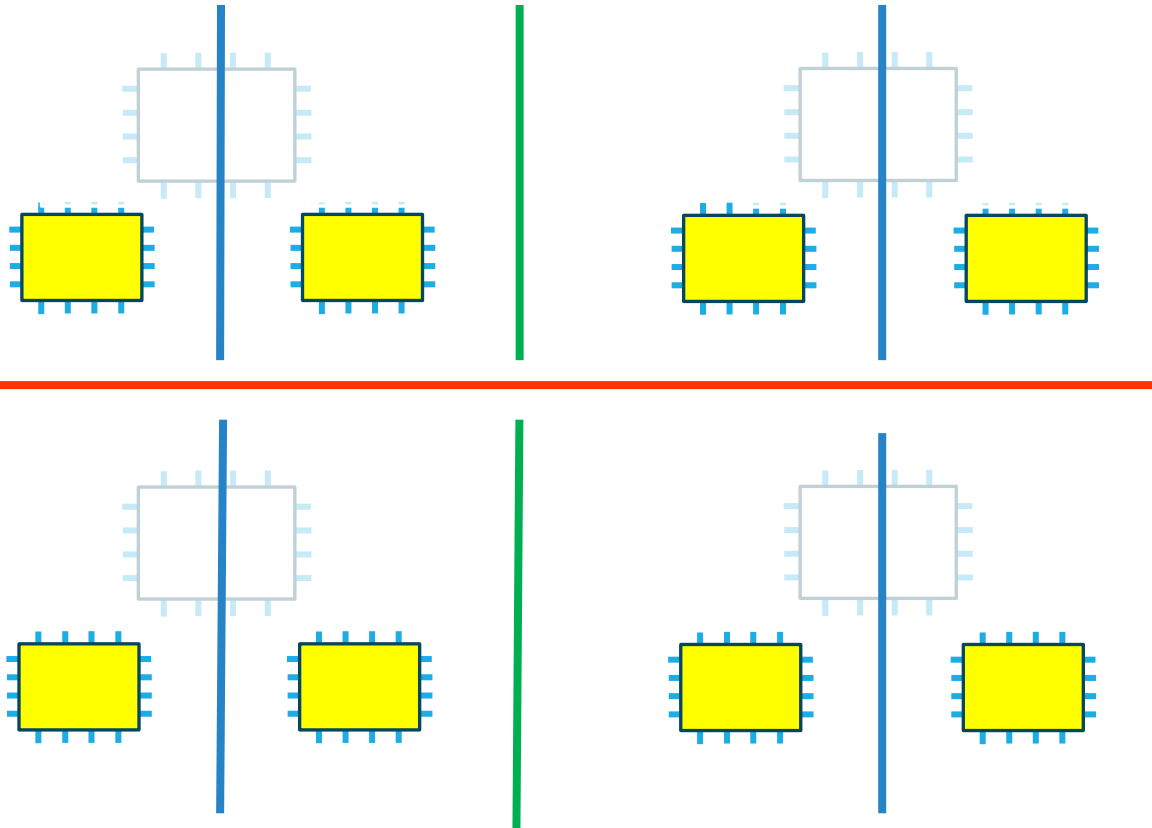
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\* Planned

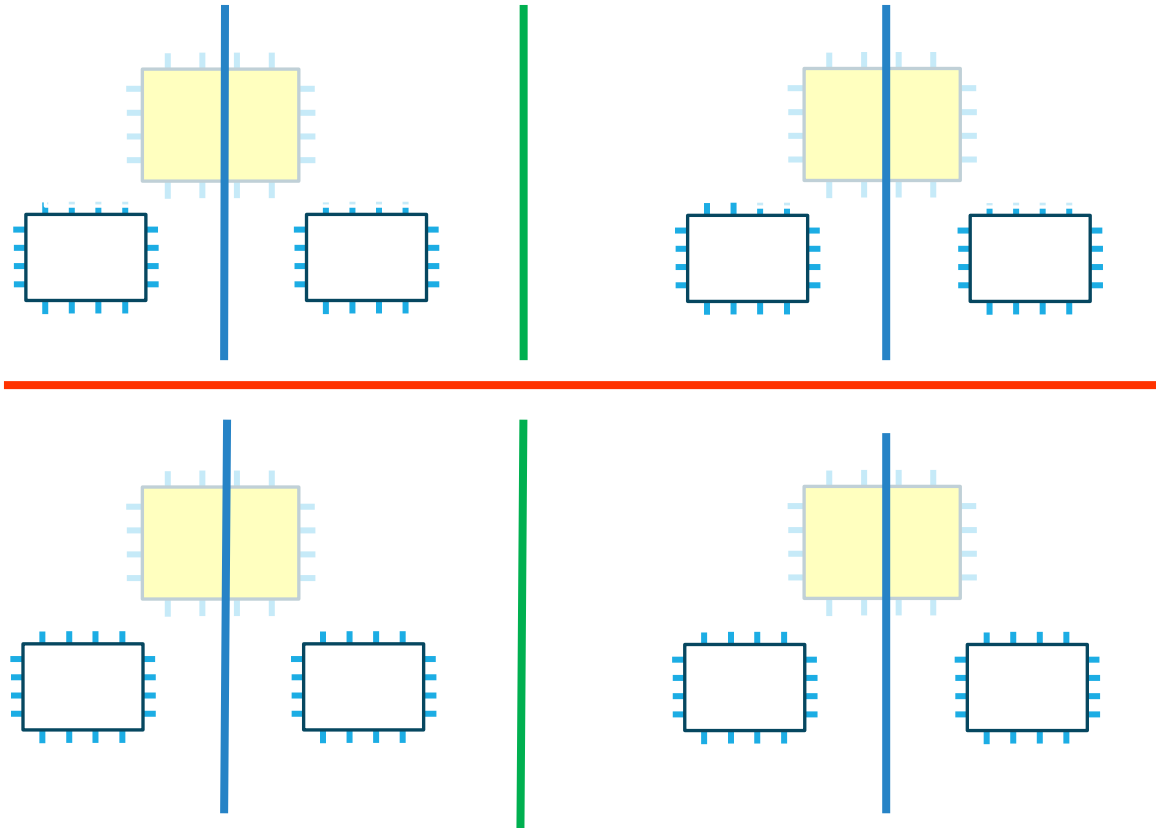
# Adding accelerators

---



# Adding accelerators

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# Assigning nodes

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```
for i in 1..4 {  
  for j = 1..8 {  
    ...  
  }  
}
```

8 nodes



# Assigning nodes

---

$W = \{2, 4, 4, 6\}$

```
for i in 1..4 <<work=W>> {  
  for j in 1..W[i]*2 {  
    ...  
  }  
}
```



# Assigning nodes

---

```
proc process_node(node) {  
  ... // Check for and process leaves  
  par {  
    task LEFT <<work=node.left.nchildren>>:  
      process_node(node.left)  
    task RIGHT <<work=node.right.nchildren>>:  
      process_node(node.right)  
  }  
}
```

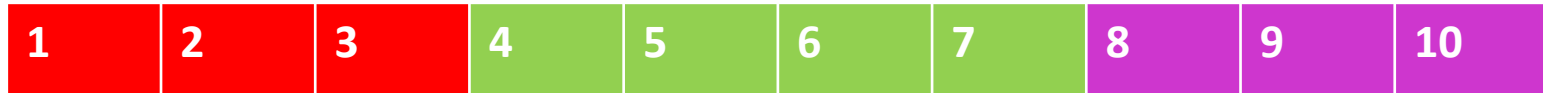
# Distributions

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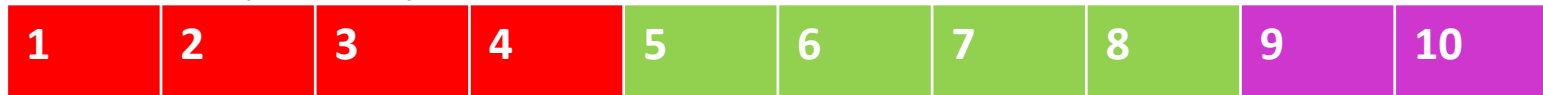
10 array elements on 3 processors



Variable Block



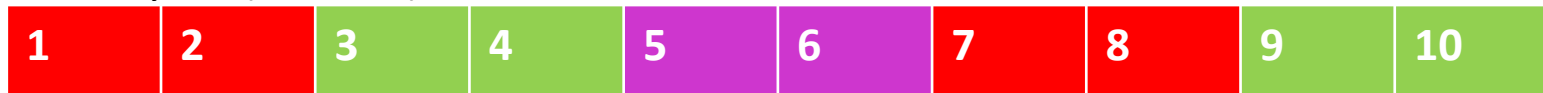
Fixed Block (block=4)



Cyclic



Block cyclic (block=2)



# Distributions

2D block cyclic execution with 2x2 block size over 7x8 grid

1,1	2,1	3,1	4,1	5,1	6,1	7,1
1,2	2,2	3,2	4,2	5,2	6,2	7,2
1,3	2,3	3,3	4,3	5,3	6,3	7,3
1,4	2,4	3,4	4,4	5,4	6,4	7,4
1,5	2,5	3,5	4,5	5,5	6,5	7,5
1,6	2,6	3,6	4,6	5,6	6,6	7,6
1,7	2,7	3,7	4,7	5,7	6,7	7,7
1,8	2,8	3,8	4,8	5,8	6,8	7,8

```
for j in [1..7,1..8] <<dist = BLOCK_CYCLIC(2)>> {  
    ...  
}
```

# Distributions

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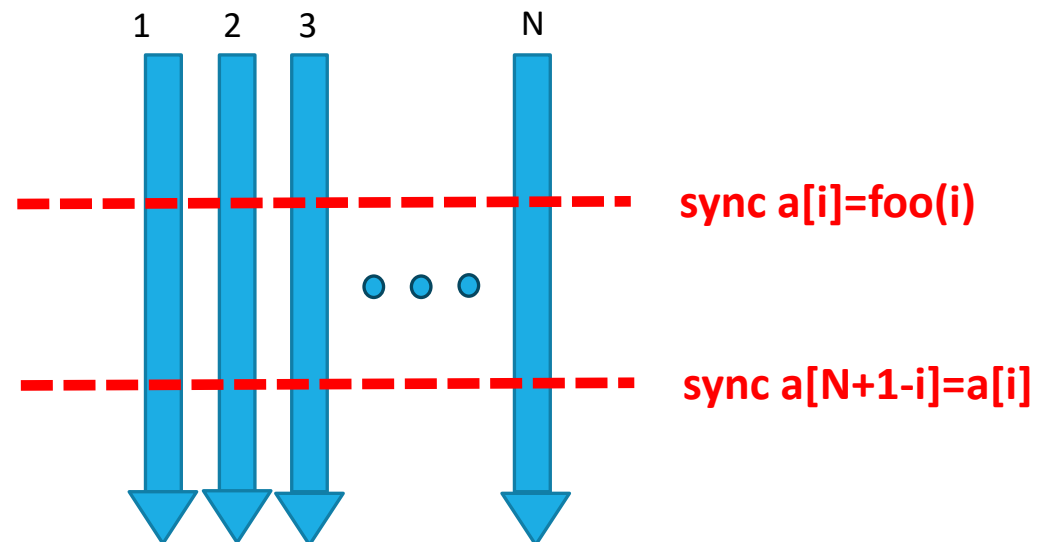
2D block cyclic array with block size of two on first dimension only over 7x8 grid

1,1	2,1	3,1	4,1	5,1	6,1	7,1
1,2	2,2	3,2	4,2	5,2	6,2	7,2
1,3	2,3	3,3	4,3	5,3	6,3	7,3
1,4	2,4	3,4	4,4	5,4	6,4	7,4
1,5	2,5	3,5	4,5	5,5	6,5	7,5
1,6	2,6	3,6	4,6	5,6	6,6	7,6
1,7	2,7	3,7	4,7	5,7	6,7	7,7
1,8	2,8	3,8	4,8	5,8	6,8	7,8

`A = array (0.0, [1..7, 1..8], [BLOCK_CYCLIC(2), ])`

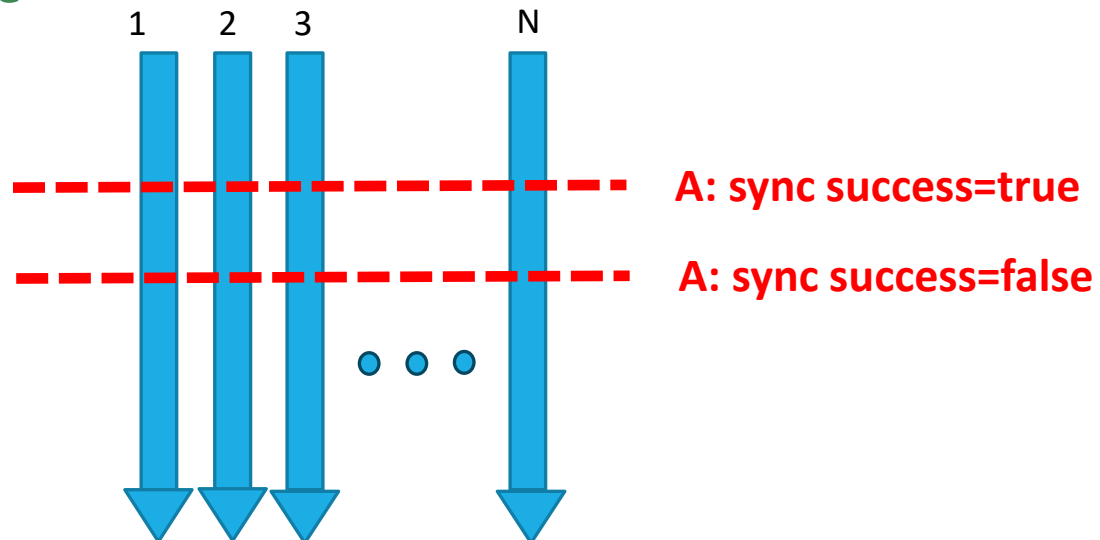
# Synchronisation

```
var a = array(0.0,[1..N])  
for i in 1..N {  
  sync a[i]=foo(i)  
  ...  
  sync a[N+1-i]=a[i]  
  ...  
}
```



# Synchronisation

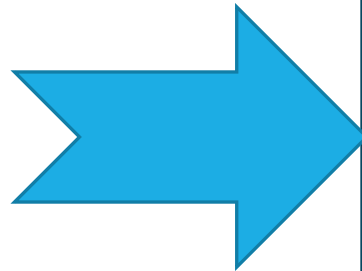
```
var success = false
for i in 1..N {
  if criterion_met(i) {
    A: sync success=true
  } elseif blocking_criterion_met(i) {
    A: sync success=false
  }
}
```





# Implementation

```
for ... {  
  if E1 {  
    S1  
    L: sync a = ...  
    S2  
  } else {  
    S3  
    L: sync b = ...  
    S4  
  }  
}
```



```
DIMENSION ...  
!OMP PARALLEL  
DO ...  
  IF E1 THEN  
    S1  
  ELSE  
    S2  
  ENDIF  
ENDDO  
!OMP END PARALLEL  
A= -> MPI  
B= -> MPI  
!OMP PARALLEL  
DO ...  
  IF E1 THEN  
    S3  
  ELSE  
    S4  
  ENDIF  
ENDDO  
!OMP END PARALLEL
```

# Scheduling

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Reorder instructions to:

- Minimise loop start/stops
- Minimise storage requirement
- Interleave computation and communication
- Merge synchronisation points

**iSend A**

**iRecv B**

**Wait**

**Process B**

**iSend C**

**iRecv D**

**Wait**

**Process D**

**Process E**

**iRecv B**

**iRecv D**

**iSend A**

**iSend C**

**Process E**

**Wait**

**Process B**

**Process D**

# PM Version 0.4

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Formal language definition released under Creative Commons Attribution 4.0 International License.

Language Implementation:

PM to FORTRAN/MPI compiler

Vector-virtual machine (intended for development/debugging)

Both available under MIT Licence

# PM Version 0.5

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A small number of language additions

- Closures
- Sparse Arrays
- Interoperability with C/FORTRAN

Added backends

- FORTRAN/MPI/OpenMP
- FORTRAN/MPI/OpenMP/OpenAcc

Planned summer 2024.

# Thank you for your attention

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Questions? T.J.Bellerby@hull.ac.uk

Follow progress: [www.pm-lang.org](http://www.pm-lang.org)

X @pmlanguage